

## The General Physical Constants.

(Reprinted by permission from the paper by R. T. Birge in *Reports on Progress in Physics*, 1941, 8, 90.)

TABLE a.

## Principal Constants and Ratios.\*

Velocity of light	$c = (2.99776 \pm 0.00004) \times 10^{10}$ cm. sec. <sup>-1</sup> .
Gravitation constant	$G = (6.670 \pm 0.005) \times 10^{-8}$ dyne cm. <sup>2</sup> g. <sup>-2</sup> .
Litre (= 1000 ml.)	$l = 1000.028 \pm 0.002$ cm. <sup>3</sup> .
Volume of ideal gas (0° C., $A_0$ )	$V_0 = (22.4146 \pm 0.0006) \times 10^3$ cm. <sup>3</sup> atmos. mol. <sup>-1</sup> .
	$V'_0 = 22.4140 \pm 0.0006$ litre atmos. mol. <sup>-1</sup> .
Volume of ideal gas (0° C., $A_{45}$ )	$V_{45} = (22.4157 \pm 0.0006) \times 10^3$ cm. <sup>3</sup> atmos. mol. <sup>-1</sup> .
	$V'_{45} = 22.4151 \pm 0.0006$ litre atmos. mol. <sup>-1</sup> .
International ohm (= $p$ abs. ohm)	$p = 1.00048 \pm 0.00002$ .
International ampere (= $q$ abs. amp.)	$q = 0.99986 \pm 0.00002$ .
Atomic weights (see table a')	
Standard atmosphere	$A_0 = (1.013246 \pm 0.000004) \times 10^6$ dyne cm. <sup>-2</sup> atmos. <sup>-1</sup> .
45° atmosphere	$A_{45} = (1.013195 \pm 0.000004) \times 10^6$ dyne cm. <sup>-2</sup> atmos. <sup>-1</sup> .
Ice-point (absolute scale)	$T_0 = 273.16 \pm 0.01^\circ$ K.
Joule equivalent	$J_{15} = 4.1855 \pm 0.0004$ abs.-joule cal. <sub>15</sub> <sup>-1</sup> .
Joule equivalent (electrical)	$J'_{15} = 4.1847 \pm 0.0003$ int.-joule cal. <sub>15</sub> <sup>-1</sup> .
Faraday constant	
(1) Chemical scale :	$F = 96501.2 \pm 10$ int.-coul. g.-equiv. <sup>-1</sup> .
	$= 96487.7 \pm 10$ abs.-coul. g.-equiv. <sup>-1</sup> .
	$= 9648.77 \pm 1.0$ abs.-e.m.u. g.-equiv. <sup>-1</sup> .
	$F' = Fc = (2.89247 \pm 0.00030) \times 10^{14}$ abs.-e.s.u. g.-equiv. <sup>-1</sup> .
(2) Physical scale :	$F = 96514.0 \pm 10$ abs.-coul. g.-equiv. <sup>-1</sup> .
	$= 9651.40 \pm 1.0$ abs.-e.m.u. g.-equiv. <sup>-1</sup> .
	$F' = Fc = (2.89326 \pm 0.00030) \times 10^{14}$ abs.-e.s.u. g.-equiv. <sup>-1</sup> .
Avogadro number (chemical scale)	$N_0 = (6.02283 \pm 0.0011) \times 10^{23}$ mol. <sup>-1</sup> .
Electronic charge	$e = F/N_0 = (1.602033 \pm 0.00034) \times 10^{-20}$ abs. e.m.u.
	$e' = ec = (4.80251 \pm 0.0010) \times 10^{-10}$ abs. e.s.u.
Specific electronic charge	$e/m = (1.7592 \pm 0.0005) \times 10^7$ abs.-e.m.u. g. <sup>-1</sup> .
	$e'/m = ec/m = (5.27368 \pm 0.0015) \times 10^{17}$ abs.-e.s.u. g. <sup>-1</sup> .
Planck constant	$h$ (see table c).

TABLE a'.

## Atomic Weights.

(1) Physical scale (<sup>16</sup>O = 16.0000).

<sup>1</sup> H = 1.00813 ± 0.00001 <sub>7</sub> .	<sup>2</sup> H = 2.01473 ± 0.00001 <sub>9</sub> .
H = 1.00827 <sub>8</sub> ± 0.00001 <sub>7</sub> (from <sup>1</sup> H/ <sup>2</sup> H abundance = 6900 ± 100).	
<sup>4</sup> He = 4.00389 ± 0.00007.	
<sup>12</sup> C = 12.00386 ± 0.00004.	<sup>13</sup> C = 13.00761 ± 0.00015.
C = 12.01465 ± 0.00023 (from <sup>12</sup> C/ <sup>13</sup> C abundance = 92 ± 2).	
<sup>14</sup> N = 14.00753 ± 0.00005.	<sup>15</sup> N = 15.0049 ± 0.0002.
N = 14.01121 ± 0.00009 <sub>5</sub> (from <sup>14</sup> N/ <sup>15</sup> N abundance = 270 ± 6).	
<sup>16</sup> O = 16.0000.	<sup>17</sup> O = 17.0045.
O = 16.00435 <sub>7</sub> ± 0.00008 <sub>6</sub> .	<sup>18</sup> O = 18.0049.
(from abundance <sup>16</sup> O : <sup>18</sup> O : <sup>17</sup> O = (506 ± 10) : 1 : (0.204 ± 0.008).	

(2) Chemical scale (O = 16.0000).

Ratio physical to chemical scale :

$r = (16.004357 \pm 0.000086)/16 = 1.000272 \pm 0.000005$ .
<sup>1</sup> H = 1.00785 <sub>8</sub> ± 0.00001 <sub>8</sub> (from physical scale).
<sup>2</sup> H = 2.01418 <sub>8</sub> ± 0.00002 <sub>1</sub> (from physical scale).
H = 1.00800 <sub>8</sub> ± 0.00001 <sub>8</sub> (from physical scale).
<sup>4</sup> He = 4.00280 ± 0.00007 (from physical scale).
C = 12.01139 ± 0.00024 (from physical scale).
N = 14.00740 ± 0.00012 (from physical scale).
N = 14.0086 ± 0.0007 (direct observation).
Na = 22.994 ± 0.003.
Cl = 35.457 ± 0.001.
Ca = 40.080 ± 0.005.
Ag = 107.880 ± 0.002.
I = 126.915 ± 0.004.

\* Unless otherwise specified, all quantities in these tables that involve the mol. or the gram equivalent are on the chemical scale of atomic weights.

TABLE b.

## Additional Quantities Evaluated or Used in Connection with Table a.

Ratio of e.s.u. to e.m.u. (direct).	
$e' = (2.9971_2 \pm 0.0001) \times 10^{10} \text{ cm.}^{1/2} \text{ sec.}^{-1/2} \text{ int.-ohm}^{1/2}.$	
$= (2.9978_4 \pm 0.0001_0) \times 10^{10} \text{ cm. sec.}^{-1}.$	
Ratio of e.s.u. to e.m.u. (indirect).	
$c' = c = (2.99776 \pm 0.00004) \times 10^{10} \text{ cm. sec.}^{-1}.$	
Average density of earth	$\delta = 5.517 \pm 0.004 \text{ g. cm.}^{-3}.$
Maximum density of water	$\delta_m(\text{H}_2\text{O}) = 0.999972 \pm 0.000002 \text{ g. cm.}^{-3}$
Acceleration of gravity (standard)	$g_0 = 980.665 \text{ cm. sec.}^{-2}.$
Acceleration of gravity ( $45^\circ$ )	$g_{45} = 980.616 \text{ cm. sec.}^{-2}.$
Density of oxygen gas ( $0^\circ \text{ C.}, A_{45}$ )	$L_1 = 1.42897 \pm 0.00003 \text{ g. litre}^{-1}.$
Limiting density of oxygen gas ( $0^\circ \text{ C.}, A_{45}$ )	$L_{\text{lim}} = 1.427609 \pm 0.000037 \text{ g. litre}^{-1}.$
Factor converting oxygen ( $0^\circ \text{ C.}, A_{45}$ ) to ideal gas	$1-a = 1.000953_5 \pm 0.000009_4.$
International coulomb (= $q$ abs. coul.)	$q = 0.99986 \pm 0.00002.$
International gauss (= $q$ abs. gauss).	
International henry (= $p$ abs. henry)	$p = 1.00048 \pm 0.00002.$
International volt (= $pq$ abs. volt)	$pq = 1.00034 \pm 0.00003.$
International joule (= $pq^2$ abs. joule)	$pq^2 = 1.00020 \pm 0.00004_5.$
Specific gravity of Hg ( $0^\circ \text{ C.}, A_0$ ) referred to air-free water at maximum density	$\rho_0 = 13.59542 \pm 0.00005.$
Density of Hg ( $0^\circ \text{ C.}, A_0$ )	$D_0 = 13.59504_0 \pm 0.00005, \text{ g. cm.}^{-3}.$
Electrochemical equivalents (chemical scale) :	
Silver (apparent)	$E_{\text{Ag}}^* = 1.11800 \times 10^{-3} \text{ g. int.-coul.}^{-1}.$
(corrected)	$E_{\text{Ag}} = (1.11807 \pm 0.00012) \times 10^{-3} \text{ g. abs.-coul.}^{-1}.$
Iodine (apparent)	$E_{\text{I}}^* = (1.315026 \pm 0.000025) \times 10^{-3} \text{ g. int.-coul.}^{-1}.$
(corrected)	$E_{\text{I}} = (1.31535 \pm 0.00014) \times 10^{-3} \text{ g. abs.-coul.}^{-1}.$
Effective calcite grating space ( $18^\circ \text{ C.}$ ), Siegbahn system	$d'_{18} = 3.02904 \times 10^{-8} \text{ cm.}$
True calcite grating space ( $20^\circ \text{ C.}$ ), Siegbahn system	$d'_{20} = 3.02951_2 \times 10^{-8} \text{ cm.}$
True calcite grating space ( $20^\circ \text{ C.}$ ), c.g.s. system	$d_{20} = (3.03567_4 \pm 0.00018) \times 10^{-8} \text{ cm.}$
Ratio of grating and Siegbahn scales of wavelengths	$\lambda_g/\lambda_s = 1.002034 \pm 0.000060.$
Density of calcite ( $20^\circ \text{ C.}$ )	$\rho = 2.71029 \pm 0.00003 \text{ g. cm.}^{-3}.$
Structural constant of calcite ( $20^\circ \text{ C.}$ )	$\phi = 1.09594 \pm 0.00001.$
Molecular weight of calcite (chemical scale)	$M = 100.091_4 \pm 0.005.$
Rydberg constant for hydrogen ( $^1\text{H}$ )	$R_{\text{H}} = 109677.581_2 \pm 0.007_5 \text{ cm.}^{-1} \text{ (I.A. scale).}$
Rydberg constant for deuterium ( $^2\text{H}$ )	$R_{\text{D}} = 109707.419_3 \pm 0.007_5 \text{ cm.}^{-1} \text{ (I.A. scale).}$
Rydberg constant for helium	$R_{\text{He}} = 109722.263 \pm 0.012 \text{ cm.}^{-1} \text{ (I.A. scale).}$
Rydberg constant for infinite mass	$R_\infty = 109737.303 \pm 0.017 \text{ cm.}^{-1} \text{ (I.A. scale),}$ $\text{or } \pm 0.05 \text{ cm.}^{-1} \text{ (c.g.s. system).}$

TABLE c.

## Partial List of Derived Quantities.†

Planck constant :

$$h = \left\{ \frac{2\pi^2 c^3 F^5}{R_\infty N_0^3 (e/m)} \right\}^{1/3} = (6.624_2 \pm 0.002_4) \times 10^{-27} \text{ erg. sec.}$$

$$h/e = \left\{ \frac{2\pi^2 c^3 F^2}{R_\infty N_0^2 (e/m)} \right\}^{1/3} = (4.1349_0 \pm 0.0007_1) \times 10^{-7} \text{ erg. sec. abs.-e.m.u.}^{-1}.$$

$$h/e' = h/ec = \left\{ \frac{2\pi^2 F^2}{R_\infty N_0^2 (e/m)} \right\}^{1/3} = (1.3793_3 \pm 0.0002_3) \times 10^{-17} \text{ erg. sec. abs.-e.s.u.}^{-1}$$

Atomic weight of electron :

$$E = F/(e/m).$$

$$\begin{aligned} \text{(physical scale)} &= (5.4862_4 \pm 0.0017) \times 10^{-4}. \\ \text{(chemical scale)} &= (5.4847_5 \pm 0.0017) \times 10^{-4}. \end{aligned}$$

Band spectra constant connecting wave number and moment of inertia :

$$h/8\pi^2 c = \left\{ \frac{F^5}{256\pi^4 R_\infty N_0^3 (e/m)} \right\}^{1/3} = (27.98_{65} \pm 0.01_0) \times 10^{-40} \text{ g. cm.}$$

Boltzmann constant :

$$k = R_0/N_0 = V_0 A_0/T_0 N_0 = (1.38047_4 \pm 0.00026) \times 10^{-16} \text{ erg. deg.}^{-1}.$$

Charge in electrolysis of one gram of H :

$$F/H = 9572.1_{73} \pm 1.0 \text{ abs.-e.m.u. g.}^{-1}.$$

Charge in electrolysis of one gram of  $^1\text{H}$  :

$$e/M_{\text{H}} = F/{}^1\text{H} = 9573.5_{60} \pm 1.0 \text{ abs.-e.m.u. g.}^{-1}.$$

† In order to be able to calculate, by propagation of errors, the probable error in a derived quantity, it is necessary to express the quantity explicitly in terms of the various fundamental quantities of Table a or of Table b, and that has been done in each case. Since in this paper  $e$  and  $h$  are treated as derived quantities, they do not therefore appear in such explicit expressions. But in calculating the numerical value of a derived quantity, the work can often be greatly simplified by using the values of other previously calculated derived quantities—in particular  $e$  and  $h$ . In order to show how certain derived quantities depend on quantities like  $e$  and  $h$ , such alternative expressions are given in many cases.

Compton shift at 90°:

$$h/mc = \left\{ \frac{2\pi^2 F^2 (e/m)^2}{R_\infty N_0^2} \right\}^{1/3} = (0.024265_{14} \pm 0.000005_7) \times 10^{-8} \text{ cm.}$$

Energy in ergs of one abs.-volt-electron:

$$E_0 = 10^8 e = 10^8 F/N_0 = (1.60203_3 \pm 0.00034) \times 10^{-12} \text{ erg}$$

Energy in calories per mol. for one abs.-volt-electron per molecule:

$$\frac{F \text{ (abs. coul. per gram-equiv.)}}{J_{15} \text{ (abs. joules per cal.)}} = 23052.8_5 \pm 3.2 \text{ cal.}_{15} \text{ mol.}^{-1}.$$

Fine structure constant:

$$\alpha = 2\pi(e')^2/hc = \left\{ \frac{4\pi R_\infty F(e/m)}{N_0} \right\}^{1/3} = (7.2976_6 \pm 0.0008_6) \times 10^{-3}.$$

$$1/\alpha = 137.030_2 \pm 0.016.$$

$$\alpha^2 = (5.3256 \pm 0.0013) \times 10^{-5}.$$

Gas constant per mol.:

$$R_0 = V_0 A_0 / T_0 = (8.31436 \pm 0.00038) \times 10^7 \text{ erg. deg.}^{-1} \text{ mol.}^{-1}.$$

$$R_0' = R_0 \cdot 10^{-7} / J_{15} = 1.98646_7 \pm 0.00021 \text{ cal.}_{15} \text{ deg.}^{-1} \text{ mol.}^{-1}.$$

$$R_0'' = V_0' / T_0 = (8.20544_7 \pm 0.00037) \times 10^{-2} \text{ litre atmos. deg.}^{-1} \text{ mol.}^{-1}.$$

$$R_0''' = R_0 / A_0 = V_0 / T_0 = 82.0566_7 \pm 0.0037 \text{ cm.}^3 \text{ atmos. deg.}^{-1} \text{ mol.}^{-1};$$

also

$$R_0 T_0 = V_0 A_0 = (2.27115_0 \pm 0.00006) \times 10^{19} \text{ erg. mol.}^{-1}.$$

Loschmidt number (0° C.  $A_0$ ):

$$n_0 = N_0 / V_0 = (2.6870_{12} \pm 0.0005_0) \times 10^{19} \text{ atmos.}^{-1} \text{ cm.}^{-3}.$$

Magnetic moment of one Bohr magneton:

$$\mu_1 = (h/4\pi)(e/m) = \frac{1}{4\pi} \left\{ \frac{2\pi^2 c^3 F^5 (e/m)^2}{R_\infty N_0^5} \right\}^{1/3} \\ = (0.9273_{45} \pm 0.0003_7) \times 10^{-20} \text{ erg. gauss}^{-1}.$$

Magnetic moment per mol. for one Bohr magneton per molecule:

$$\mu_1 N_0 = \frac{1}{4\pi} \left\{ \frac{2\pi^2 c^3 F^5 (e/m)^2}{R_\infty N_0^2} \right\}^{1/3} = 5585.2_4 \pm 1.6 \text{ erg. gauss.}^{-1} \text{ mol.}^{-1}.$$

Mass of  $\alpha$ -particle:

$$M_\alpha = (\text{He} - 2E)/N_0 = (6.6442_2 \pm 0.0012) \times 10^{-24} \text{ g.}$$

Mass of atom of unit atomic weight:

$$M_0 = 1/N_0 = (1.66035 \pm 0.00031) \times 10^{-24} \text{ g.}$$

Mass of electron:

$$m = e/(e/m) = (F/N_0)/(e/m) = (9.1066_0 \pm 0.0032) \times 10^{-28} \text{ g.}$$

Mass of  $^1\text{H}$  atom:

$$M_{1\text{H}} = {}^1\text{H}/N_0 = (1.67339_3 \pm 0.00031) \times 10^{-24} \text{ g.}$$

Mass of proton:

$$M_P = ({}^1\text{H} - E)/N_0 = (1.67248_2 \pm 0.00031) \times 10^{-24} \text{ g.}$$

Radiation density constant:

$$\alpha = 8\pi^5 k^4 / 15c^3 h^3 = \left( \frac{V_0 A_0}{T_0} \right) \frac{4\pi N_0^3 R_\infty (e/m)}{15c^6 F^5} = (7.569_{42} \pm 0.004_6) \times 10^{-15} \text{ erg. cm.}^{-3} \text{ deg.}^{-4}.$$

Ratio mass  $^1\text{H}$  atom to mass electron:

$$M_{1\text{H}}/m = (e/m)({}^1\text{H}/F) = 1837.5_{61} \pm 0.5_6.$$

Ratio mass proton to mass electron:

$$M_P/m = (e/m) \left( \frac{{}^1\text{H} - E}{F} \right) = 1836.5_{61} \pm 0.5_6.$$

Second radiation constant:

$$c_2 = hc/k = \frac{T_0 c^2}{V_0 A_0} \left\{ \frac{2\pi^2 F^5}{R_\infty N_0^2 (e/m)} \right\}^{1/3} = 1.4384_8 \pm 0.0003_4 \text{ cm. deg.}$$

Specific charge of  $\alpha$ -particle:

$$2e/M_\alpha = \frac{2F}{\text{He} - 2E} = 4822.3_3 \pm 0.5_1 \text{ abs.-e.m.u. g.}^{-1}.$$

Specific charge of proton:

$$e/M_P = \frac{F}{{}^1\text{H} - E} = 9578.7_7 \pm 1.0 \text{ abs.-e.m.u. g.}^{-1}.$$

Stefan-Boltzmann constant:

$$\sigma = ac/4 = 2\pi^5 k^4 / 15c^2 h^3 = \left( \frac{V_0 A_0}{T_0} \right) \frac{4\pi^3 N_0 R_\infty (e/m)}{15(Fc)^5} \\ = (5.672_{83} \pm 0.003_7) \times 10^{-5} \text{ erg. cm.}^{-2} \text{ deg.}^{-4} \text{ sec.}^{-1}.$$

Wave-length associated with one abs. volt :

$$\lambda_0 = 10^{-8} c^2 (h/e^2) = \frac{c^2}{10^8} \left\{ \frac{2\pi^2 F^2}{R_\infty N_0^2 (e/m)} \right\}^{1/3} = (12395.4 \pm 2.1) \times 10^{-8} \text{ cm. abs.-volt.}$$

Wave number associated with one abs. volt :

$$s_0 = 1/\lambda_0 = \frac{10^8}{c^2} \left\{ \frac{R_\infty N_0^2 (e/m)}{2\pi^2 F^2} \right\}^{1/3} = 8067.4_8 \pm 1.4 \text{ cm.}^{-1} \text{ abs.-volt}^{-1}.$$

Wien's displacement-law constant : \*

$$A = c_2/4.965114 = 0.28971_8 \pm 0.00007 \text{ cm. deg.}$$

Zeeman displacement per gauss :

$$(e/m)/4\pi c = (4.6699_1 \pm 0.0013) \times 10^{-5} \text{ cm.}^{-1} \text{ gauss.}^{-1}.$$

\* The factor 4.965114 is the root of  $e^{-\beta} + (\beta/5) - 1 = 0$ .

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